# CBSE NCERT Solutions for Class 10 mathematics Chapter 14

#### Exercise 14.1

Q.1. A survey was conducted by a group of students as a part of their environment awareness program, in which they collected the following data regarding the number of plants in 20 houses in a locality. Find the mean number of plants per house.

Number of plants	0-2	2-4	4-6	6-8	8-10	10-12	12-14
Number of houses	1	2	1	5	6	2	3

Which method did you use for finding the mean, and why?

Solution: First of all, we have to find class marks xi for each interval.

We know that, class mark(xi)=upper class limit+lower class limit2

Now we may compute xi and fixi as following

Number of plants Number of houses fi		xi	fixi
0-2	1	1	1×1=1
2-4 4-6	2	3	2×3=6
4-6	1	5	1×5=5
6-8	5	7	5×7=35
8-10	6	9	6×9=54
10-12	2	11	2×11=22
12-14	3	13	3×13=39
Total	20		162

From the table, we can see that Σfi=20 Σfixi=162

Mean x-=ΣfixiΣfi

=16220=8.1

Hence, mean number of plants per house is 8.1. Direct method is used here as values of class marks xi and fi are small.

Q.2. Consider the following distribution of daily wages of 50 workers of a factory.

Daily wages (in₹)	500-520	520-540	540-560	560-580	580-600
Number of workers	12	14	8	6	10

Find the mean daily wages of the workers of the factory by using an appropriate method.

We will use step deviation method.

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First, we have to find class mark for each interval.

We know that, xi=upper class limit+lower class limit2 Class size (h) of this data =20. Let us take 550 as assumed mean (a). Now, we can calculate di,ui and fiui as following:

Daily wages (in₹)	Number of workers fi	xi	di=xi-550	ui=xi-550h	fiui
500-520	12	510	-40	-2	-24
520-540	14	530	-20	-1	-14
540-560	8	550	0	0	0
560-580	6	570	20	1	6
580-600	10	590	40	2	20
Total	50				-12

From the table, we can see that,

 $\Sigma fi=50$ 

Σfixi=-12 Mean x-=a+ΣfiuiΣfih =550+-125020 =550-245 =550-4.8 =545.2 So, mean daily wages of the workers of the factory is ₹545.20.

Q.3. The following distribution shows the daily pocket allowance of children of a locality. The mean pocket allowance is ₹ 18. Find the missing frequency f.

Daily pocket allowance (in ₹)	11-13	13-15	15-17	17-19	19-21	21-23	23-25
Number of workers	7	6	9	13	f	5	4

Solution:

First, we have to find class mark for each interval.

We know that,

Classmarkxi=upper class limit+lower class limit2

Mean pocket allowance x-₹18 ....... (Given) Let us take 18 as assumed mean (a). Now we can calculate di and fidi as

following

Daily pocket allowance (in ₹)	Number of children fi	Class mark xi	di=xi-18	fidi
11-13	7	12	-6	-42
13-15	6	14	-4	-24
15-17	9	16	-2	-18
17-19	13	18	0	0
19-21	f	20	2	2f
21-23	5	22	4	20
23-25	4	24	6	24
Total	∑fi=44+f			2f-40

From the table we can see that

Σfi=44+f ----(1)

 $\Sigma$ fidi=2f-40 -----(2)x =a+ $\Sigma$ fidi $\Sigma$ fi ------(3)Now put the values of  $\Sigma$ fi and  $\Sigma$ fidi from equations (1) and (2) to equation (3) 18=18+2f-4044+f On solving, we get 0=2f-4044+f 2f-40=0 2f=40 f=20 Hence, the missing frequency f is 20.

Q.4. Thirty women were examined in a hospital by a doctor and the number of heart beats per minute were recorded and summarized as follows. Find the mean heart beats per minute for these women, choosing a suitable method.

Number of heart beats per minute	65-68	68-71	71-74	74-77	77-80	80-83	83-86
Number of women	2	4	3	8	7	4	2

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Page 2 of 19

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We will use step deviation method.

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First of all, we have to find class mark for each interval.

We know that, Classmarkxi=upper class limit+lower class limit2 Class size(h) of this data =3 Let us take 75.5 as assumed mean (a). Now we can calculate di,ui and fiui as following.

Number of heart beats per minute	Number of women fi	xi	di=xi-75.5	ui=xi-75.5h	fiui
65-68	2	66.5	-9	-3	-6
68-71	4	69.5	-6	-2	-8
71-74	3	72.5	-3	-1	-3
74-77	8	75.5	0	0	0
77-80	7	78.5	3	1	7
80-83	4	81.5	6	2	8
83-86	2	84.5	9	3	6
Total	30	1			4

Now, we can see from table that

Σfi=30

 $\Sigma \text{fiui} = \frac{4 \text{ Mean x} - \text{a} + \Sigma \text{fiui} \Sigma \text{fih}}{1 \text{ Mean x} - \text{a} + \Sigma \text{fiui} \Sigma \text{fih}} = 75.5 + 430 \times 3 = 75.5 + 0.4 = 75.9 \text{ So, mean heart beats per minute}$  where  $\frac{1}{2} \times \frac{1}{2} \times \frac{1}{$ 

Q.5. In a retail market, fruit vendors were selling mangoes kept in packing boxes. These boxes contained varying number of mangoes. The following was the distribution of mangoes according to the number of boxes.

Number of mangoes	50-52	53-55	56-58	59-61	62-64
Number of boxes	15	110	135	115	25

Find the mean number of mangoes kept in a packing box. Which method of finding the mean did you choose?

Number of mangoes	Number of boxes fi
50-52	15
53-55	110
56-58	135
59-61	115
62-64	25

There is a gap of 1 between any two consecutive class intervals. So, we can say that class intervals are not continuous. In order to remove this problem, we have to add 12 to upper class limit and subtract 12 from lower class limit of each interval.

Now we will use step deviation method.

Class mark (xi) may be obtained by using the relation

Classmarkxi=upper class limit+lower class limit2 Class size (h) of this data =3 Let us take 57 as assured mean (a). Now we can calculate di,ui and fiui as following.

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Class interval	fi	xi	di=xi-57	ui=xi-57h	fiui
49.5-52.5	15	51	-6	-2	-30
52.5-55.5	110	54	-3	-1	-110
55.5-58.5	135	57	0	0	0
58,5-61,5	115	60	3	1	115
61.5-64.5	25	63	6	2	50
Total	400				25

Now, we can see that

Σfi=400

Σfiui=25 Mean x =a+ΣfiuiΣfi×h

=57+25400×3

=57+316=57+0.1875

=57.1875

=57.19 So, mean number of mangoes kept in a packing box is 57.19. Here, we chose step deviation method as values of fi,di are big and also there is a common multiple (3) between all di.

Q.6. The table below shows the daily expenditure on food of 25 households in a locality.

Daily expenditure (in ₹)	100-150	150-200	200-250	250-300	300-350
Number of households	4	5	12	2	2

Find the mean daily expenditure on food by a suitable method.

Solution:

We will use step deviation method.

First of all, we have to find class mark for each interval.

We know that, Class markxi=upper class limit+lower class limit2 Class size (h)=50 Let us take 225 as assumed mean (a). Now we can calculate di,ui and fiui as following.

Daily expenditure (in ₹)	fi	xi	di=xi-225	ui=xi-225h	fiui
100-150	4	125	-100	-2	-8
150-200	5	175	-50	-1	-5
200-250	12	225	0	0	0
250-300	2	275	50	1	2
300-350	2	325	100	2	4
Total	25				-7

Now, we can see that

Σfi=25

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Q.7. To find out the concentration of SO2 in the air (in parts per million, i.e., ppm), the date (INTADADE MY) certain city and is presented below:

Concentration of SO2 (in pmm)	Frequency
0.00-0.04	4
0.04-0.08	9
0.08-0.12	9
0.12-0.16	2
0.16-0.20	4
0.20-0.24	2

Find the mean concentration of SO2 in the air.

Solution: We will use step deviation method.

First of all, we have to find class mark for each interval.

We know that, Class markxi=upper class limit+lower class limit2 Class size (h)=0.04 Let us take 0.14 as assumed mean (a). Now we can calculate di,ui and fiui as following.

Concentration of SO2 (in ppm)	Frequency fi	Class mark xi	di=xi-0.14	ui=xi-0.14h	fiui
0.00-0.04	4	0.02	-0.12	-3	-12
0.04-0.08	9	0.06	-0.08	-2	-18
0.08-0.12	9	0.10	-0.04	-1	-9
0.12-0.16	2	0.14	0	0	0
0.16-0.20	4	0.18	0.04	1	4
0.20-0.24	2	0.22	0.08	2	4
Total	30				-31

From the table, we can see that

Σfi=30

 $\Sigma \text{fiui}=-31 \text{ Mean, } x=a+\Sigma \text{fiui} \Sigma \text{fih}=0.14+-3130\times0.04=0.14-0.04133=0.09867=0.099ppm Hence, mean concentration of SO2 in the air is 0.099ppm.$ 

Q.8. A class teacher has the following absentee record of 40 students of a class for the whole term. Find the mean number of days a student was absent.

Number of days	0-6	6-10	10-14	14-20	20-28	28-38	38-40
Number of students	11	10	7	4	4	3	1

We will use shortcut method or assumed mean method.

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First of all, we have to find class mark for each interval.

We know that, Class markxi=upper class limit+lower class limit2 Let us take 17 as assumed mean (a). We can calculate di and fidi as following

Number of days	Number of students fi	xi	di=xi-17	fidi
0-6	11	3	-14	-154
6-10	10	8	-9	-90
10-14	7	12	-5	-35
14-20	4	17	0	0.
20-28	4	24	7	28
28-38	3	33	16	48
38-40	1	39	22	22
Total	40			-181

Now, we can see that

Σfi=40

 $\Sigma$ fidi=-181 Mean x-=a+ $\Sigma$ fidi $\Sigma$ fi =17+-18140 =17-4.525 =12.475 =12.48 Hence, mean number of days for which a student was absent is 12.48 days.

Q.9. The following table gives the literacy rate (in percentage) of 35 cities. Find the mean literacy rate.

Literacy rate (in %)	45-55	55-65	65-75	75-85	85-95
Number of cities	3	10	11	8	3

Solution:

We will use step deviation method.

First of all, we have to find class mark for each interval.

We know that, Class markxi=upper class limit+lower class limit2 Class size(h) for this data =10. Let us take 70 as assumed mean a, we can calculate di, ui, and fiui as following

Literacy rate (in %)	Number of cities fi	xi	di=xi-70	ui=dih	fiui
45-55	3	50	-20	-2	-6
55-65	10	60	-10	-1	-10
65-75	11	70	0	0	0
75-85	8	80	10	1	8
85-95	3	90	20	2	6
Total	35	Г			-2

Now, we can see that

Σfi=35

Σfiui=-2 Mean x-=a+ΣfiuiΣuih =70+-235×10 =70-2035 =70-0.57 =69.43 So, mean literacy rate is 69.43%.

#### Exercise 14.2

Q.1. The following table shows the ages of the patients admitted in a hospital during a year:

Age (in years)	5-15	15-25	25-35	35-45	45-55	55-65
Number of patients	6	11	21	23	14	5

Find the mode and the mean of the data given above. Compare and interpret the two measures of central tendency.

Solution:

We will use shortcut or assumed mean method.

First of all, we have to find class mark for each interval.

We know that, xi=upper class limit+lower class limit2 Now, let us take 30 as assumed mean (a), we can calculate di and fidi as following.

Age (in years)	Number of patients fi	Class mark xi	di=xi-30	fidi
5-15	6	10	-20	-120
15-25	11	20	-10	-110
25-35	21	30	0	0
35-45	23	40	10	230
45-55	14	50	20	280
55-65	5	60	30	150

From the table, we may observe that

∑ fi=80

 $\sum$  fidi=430 Mean x-=a+ $\sum$  fidi $\sum$   $\sum$ fi =30+43080 =30+5.375 =35.375 =35.38 Clearly, mean of this data is 35.38 which means that the average age of a patient admitted to hospital was 35.38 years.

As we can see that maximum class frequency is 23 which belongs to class interval 35-45.

So, modal class =35-45

Lower limit (l) of modal class =35 Frequency (f1) of modal class =23 Class size (h) =10 Frequency (f0) of class preceding the modal class =21 Frequency (f2) of class succeeding the modal class =14 Now, mode =1+f1-f02f1-f0-f2×h =35+23-21223-21-14×10 =35+2011 =35+1.81 =36.8 Clearly, mode is 36.8. It represents that maximum number of patients admitted in hospital were of 36.8 years.

Q.2. The following data gives information on the observed lifetimes (in hours) of 225 electrical components:

Lifetimes (in hours)	0-20	20-40	40-60	60-80	80-100	100-120
Frequency	10	35	52	61	38	29

Determine the modal lifetimes of the components.

Solution:

From the given data, it is clear that maximum class frequency is 61 which belongs to class interval 60-80.

So, modal class =60-80

Lower class limit (I) of modal class =60 Frequency (f1) of modal class =61 Frequency (f0) of class preceding the modal class =52 Frequency (f2) of class succeeding the modal class =38 Class size (h)=20

Mode = 1+f1-f02f1-f0-f2×h

=60+61-52261-52-38×20

=60+9122-9020 =60+93220 =60+9016=60+5.625 =65.625 So, modal lifetime of electrical components is 65.625 hours.

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Q.3. The following data gives the distribution of total monthly household expenditure of 2 KRANTIADADE MAY monthly expenditure of the families. Also, find the mean monthly expenditure.

Expenditure (in ₹)	Number of families
1000-1500	24
1500-2000	40
2000-2500	33
2500-3000	28
3000-3500	30
3500-4000	22
4000-4500	16
4500-5000	7

Solution:

From the given data, it is clear that maximum class frequency is 40 which belongs to 1500-2000 intervals.

So, modal class =1500-2000

Lower limit (l) of modal class = 1500 Frequency (f1) of modal class = 40 Frequency (f0) of class preceding modal class = 24 Frequency (f2) of class succeeding modal class = 33 Class size h=500

Mode=I+f1-f02f1-f0-f2×h

=1500+40-24240-24-33×500

=1500+1680-57500 =1500+800023 =1500+347.826 =1847.826=1847.83 So, modal monthly expenditure was ₹ 1847.83

Now, we have to find class mark

Classmark=upper class limit+lower class limit2

Class size (h) of give data =500 Let us take 2750 as assumed mean a, we can calculate diui and fiui as following

Expenditure (in ₹)	Number of families fi	xi	di=xi-2750	ui=xi-2750h	fiui
1000-1500	24	1250	-1500	-3	-72
1500-2000	40	1750	-1000	-2	-80
2000-2500	33	2250	-500	-1	-33
2500-3000	28	2750	0	0	0
3000-3500	30	3250	500	1	30
3500-4000	22	3750	1000	2	44
4000-4500	16	4250	1500	3	48
4500-5000	7	4750	2000	4	28
Total	200				-35

Now, from the table it is clear that

∑ fi=200 ∑ fiui=-35

x-(mean)=a+∑ fiui∑ fi×h x-=2750+-35200×500 =2750-87.5 =2662.5 So, mean monthly expenditure was ₹ 2662.50.

Q.4. The following distribution gives the state-wise teacher-student ratio in higher secondary schools of India. Find the mode and mean of this data. Interpret the two measures.

12.20	2
15-20	3
20-25	8
25-30	9
30-35	10
35-40	3
40-45	0
45-50	0
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From the given data, it is clear that maximum class frequency is 10 which VERANTADADEMY

So, modal class =30-35

Class size h=5 Lower limit (l) of modal class =30 Frequency (f1) of modal class =10 Frequency (f0) of class preceding modal class =9 Frequency (f2) of class succeeding modal class =3

Mode=l+f1-f02f1-f0-f2×h

=30+10-9210-9-3×5

=30+120-125

=30+58=30.625

Mode=30.6

It represents that teacher student ratio of most of states/U.T is 30.6.

Now, we will use step deviation method to find mean.

We have to find out class mark by using the relation

Classmark=upper class limit+lower class limit2 Let us take 32.5 as assumed mean. We can calculate di,ui and fiui as following.

Number of student per teacher	Number of states/U.T fi	xi	di=xi-32.5	ui=xi-32.5h	fiui
15-20	3	17.5	-15	-3	-9
20-25	8	22.5	-10	-2	-16
25-30	9	27.5	-5	-1	-9
30-35	10	32.5	0	0	0
35-40	3	37.5	5	1	3
40-45	0	42.5	10	2	0
45-50	0	47.5	15	3	0
50-55	2	52.5	20	4	8
Total	35				-23

Now, mean x-=a+ΣfiuiΣfih

=32.5+-2335×5

=32.5-237=32.5-3.28

=29.22

So, mean of data is 29.2 which means that on an average teacher-student ratio was 29.2.

Q.5. The given distribution shows the number of runs scored by some top batsmen of the world in one-day international cricket matches.

Number of students per teacher	Number of states/UT
3000-4000	4
4000-5000	18
5000-6000	9
6000-7000	7
7000-8000	6
8000-9000	3
9000-10000	1
10000-11000	1

Find the mode of the data.

Solution: It is clear from the given data that maximum class frequency is 18 which MIKRANITADADEMY

So, modal class =4000-5000

Lower limit (l) of modal class =4000 Frequency (f1) of modal class =18

Frequency (f0) of class preceeding modal class =4

Frequency (f2) of class succeeding modal class =9

Class size h=1000

Now, Mode=l+f1-f02f1-f0-f2×(h)

=4000+18-4218-4-9×1000

=4000+1400023

=4000+608.695

=4608.695

So mode of given data is 4608.7 runs.

Q.6. A student noted the number of cars passing through a spot on a road for 100 periods each of 3 minutes and summarized it in the table given below. Find the mode of the data:

Number of cars	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
Frequency	7	14	13	12	20	11	15	8

Solution: It is clear from the given data that maximum class frequency is 20 which belongs to 40-50 class intervals.

So, modal class =40-50

Lower limit (l) of modal class =40 Frequency (f1) of modal class =20 Frequency (f0) of class preceding modal class =12 Frequency (f2) of class succeeding modal class =11 Class size =10

Mode=l+f1-f02f1-f0-f2×(h)

=40+20-12220-12-11×10 =40+8040-23

=40+8017 =40+4.7 So, mode of this data is 44.7 cars.

#### Exercise 14.3

Q.1. The following frequency distribution gives the monthly consumption of electricity of 68 consumers of a locality. Find the median, mean and mode of the data and compare them.

Monthly consumption (in units)	Number of consumers
65 - 85	4
85 - 105	5
105 - 125	13
125 - 145	20
145 - 165	14
165 - 185	8
185 - 205	4

Solution:

First of all, we have to find class mark for each interval.

We know that,

Classmark=Upper class limit+Lower class limit2 Let us take 135 as assumed mean (a), according to step deviation method we may find di,ui,fi×ui, as following

Monthly consumption (in units)	Number of consumers fi	Xi class mark	di=xi-135	u1=d120	fiui
65 - 85	4	75	-60	-3	-12
85 - 105	5	95	-40	-2	-10
105 - 125	13	115	-20	-1	-13
125 - 145	20	135	0	0	0
145 - 165	14	155	20	1	14
165 - 185	8	175	40	2	16
185 - 205	4	195	60	3	12
Total	68			1	7

We can observe from the table

Sfiui=7

∑fi=68 Class size h=20 Mean x-a+∑fiui∑fi×h

=135+768×20

=135+14068

=137.058

It is clear from the table that maximum class frequency is 20 which belongs to the class interval 125-145.

Modal class =125-145

Lower limit (l) of modal class =125 Class size (h)=20 Frequency (fl) of modal class=20 Frequency (fl) of class preceding modal class=13 Frequency (fl) of class succeeding the modal class=14 Mode=l+fl-fl02fl-fl0-f2×h

=125+20-13220-13-14×20

=125+713×20

=125+14013=135.76

We know that,

3 median = mode + 2 mean

=135.76+2(137.058) =135.76+274.116 =409.876  $\Rightarrow$  Median =409.8763 Median =136.625 Therefore, the median, mode, mean of given data is 136.625, 135.76, 137.05 respectively.

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Page 11 of 19

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Q.2. If the median of the distribution given below is 28.5, find the values of x and y.

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Class interval	Frequency	
0 - 10	5	
10 - 20	x	
20 - 30	20	
30 - 40	15	
40 - 50	у	
50 - 60	5	
Total	60	

Solution:

First of all, we have to find cumulative frequency of the given data.

Class interval	Frequency	Cumulative frequency
0 - 10	5	5
10 - 20	х	5+x
20 - 30	20	25+x
30 - 40	15	40+x
40 - 50	У	40+x+y
50 - 60	5	45+x+y
Total (n)	60	

It is clear that n=60

45+x+y=60

x+y=15 ......(1) Median of data =28.5 ....... (given) Median of data lies in interval 20-30. So, median class =20-30. Lower limit 1 of median class =20. Cumulative frequency (cf ) of class preceding the median class =5+x Frequency (f) of median class =20. Class size (h)=10.

Now, median =1+n2-cff×h

28.5=20+602-5+x20×10

8.5=25-x2 17=25-x x=8 Put the value of x in equation (1) 8+y=15 y=7 Hence, values of x and y are 8 and 7 respectively.

Q.3. A life insurance agent found the following data for distribution of ages of 100 policy holders. Calculate the median age, if policies are given only to persons having age 18 years onwards but less than 60 year.

Age (in years)	Number of policy holders
Below 20	2
Below 25	6
Below 30	24
Below 35	45
Below 40	78
Below 45	89
Below 50	92
Below 55	98
Below 60	100

We can see from above table that class width is not same. We don't need that the same with upper class limits and is of less than type. As policies were given only to persons having age 18 years onwards but less than 60 years, we can define the class intervals with their respective cumulative frequency as given below.

Age (in years)	Number of policy holders fi	Cumulative frequency Cf
18-20	2	2
20-25	6-2=4	6
25-30	24-6=18	24
30-35	45-24=21	45
35-40	78-45=33	78
40-45	89-78=11	89
45-50	92-89=3	92
50-55	98-92=6	98
55-60	100-98=2	100
Total n		

We can see from the table that n=100.

n2=50

Cumulative frequency (cf) just greater than n2 is 78. n2=50 It belongs to interval 35 – 40 So, median class = 35 – 40 Lower limit (l) of median class =35 Class size (h)=5 Frequency (f) of median class =33 Cumulative frequency (cf) of class preceding median class =45 median =l+n2-cff×h =35+50-4533×5 =35+2533 =35.76 So, median age is 35.76 years.

Q.4. The lengths of 40 leaves of a plant are measured correct to the nearest millimeter, and the data obtained is represented in the following table:

Length (in mm)	Number or leaves fi
118 –126	3
127 – 135	5
136 – 144	9
145-153	12
154 – 162	5
163-171	4
172-180	2

Find the median length of the leaves.

(Hint: The formula is for continuous classes only so we have to convert the given data into continuous classes for finding the median. The classes then change to 117.5-126.5, 126.5-135.5, -171.5-180.5)

Solution:

The given data does not have continuous class intervals. We can observe from the table that difference between two class intervals is 1. So, we have to add 0.5 to upper class limits and subtract 0.5 to lower class limits.

Now continuous class intervals with respective cumulative frequencies can be represented as below.

Length (in mm)	Number or leaves fi	Cumulative frequency
117.5 -126.5	3	3
126.5 - 135.5	5	3 + 5 = 8
135.5 - 144.5	9	8 + 9 = 17
144.5-153.5	12	17 + 12 = 29
153.5 - 162.5	5	29 + 5 = 34
162.5-171.5 4		34 + 4 = 38
171.5-180.5	2	38 + 2 = 40

Here, n = 40

We can observe from the table that cumulative frequency just greater then n2 is 20.

It belongs to class interval 144.5 - 153.5. So, median class = 144.5 - 153.5 Lower limit (I) of median class = 144.5 Class size (h) = 9 Frequency (f) of median class = 12 Cumulative frequency (cf) of class preceding median class = 12 Cumulative frequency (cf) of class preceding median class = 12 Cumulative frequency (cf) of class preceding median class = 144.5 ± 20 ± 171.2 × 9 = 144.5 ± 9.4 ± 146.75. So, median length of leaves.

Call: +91- 9686 1083 lass 421 Median = 1+n2-cff + page 13-81 119 ×9 = 144.5+94=146.75 Source landenest of leaveny.org

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is 146.75 mm.

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Q.5. Find the following, the given table depicts the distribution of the lifetime of 400 neon lamps:

Lifetime (in hours)	Number of lamps
1500 - 2000	14
2000 - 2500	56
2500 - 3000	60
3000 - 3500	86
3500 - 4000	74
4000 - 4500	62
4500 - 5000	48

Find the median lifetime of a lamp.

Solution: First, we have to find cumulative frequencies with their respective class intervals.

Lifetime (in hours)	Number of lamps	Cumulative frequency	
1500 - 2000	14	14	
2000 - 2500	56	14+56=70	
2500 - 3000	60	70+60=130	
3000 - 3500	86	130+86=216	
3500 - 4000	74	216+74=290	
4000 - 4500	62	290+62=352	
4500 - 5000	48	352+48=400	
Total (n)	400		

Here, n=400

So, n2=200

From the table, we can observe that cumulative frequency just greater than n2(i.e.,4002=200) is 216. It belongs to class interval 3000-3500.

So, Median class =3000-3500

Lower limit (I) of median class =3000 Frequency (f) of median class =86 Cumulative frequency (cf) of class preceding median class =130 Class size h=500 Median=I+n2-cff×h=3000×200-13086×500=3000+70×50086 =3000+406.976 =3406.976 So, median lifetime of lamps is 3406.98 hours.

Q.6. 100 surnames were randomly picked up from a local telephone directory and the frequency distribution of the number of letters in the English alphabets in the surnames was obtained as follows:

Number of letters	1 - 4	4-7	7-10	10-13	13-16	16-19
Number of surnames	6	30	40	16	4	4

Determine the median number of letters in the surnames. Find the mean number of letters in the surnames? Also, find the modal size of the surnames.

First of all, we have to find cumulative frequencies with their respective clyster ANTADADEMY

Number of letters	Frequency fi	Cumulative frequency
1-4	6	6
4-7	30	30+6=36
7-10	40	36+40=76
10-13	16	76+16=92
13-16	4	92+4=96
16-19	4	96+4=100
Total n	100	ĺ

Here, n=100.

So, n2=50

From the table, we can observe that cumulative frequency is 50. It belongs to class interval 7-10. So, median class =7-10 Lower limit (l) of median class =7 Cumulative frequency (cf) of class preceding median class =36 Frequency (f) of median class =40 Class size (h)=3 Median=1+n2-cff×h=7+50-3640×3=7+14×340=7+1.05 =8.05

Now, we have to find class marks of given class intervals by using relation

Classmark=Upper class limit+lower class limit2

Taking 11.5 as assumed mean (a) we can find di, ui and fi, ui according to step deviation method as below.

Number of letters	Number of surnames	xi	xi-a	ui=xi-a3	fiui
1-4	6	2.5	-9	-3	-18
4-7	30	5.5	-6	-2	-60
7-10	40	8.5	-3	-1	-40
10-13	16	11.5	0	0	0
13-16	4	14.5	3	1	4
16-19	4	17.5	6	2	8
Total	100			. 7	-106

∑fiui=-106

∑fi=100

Mean  $=x-a+(\sum fiui \sum fi)h = 11.5+.106100 \times 3 = 11.5-3.18=8.32$  We know that, 3 median = mode +2 mean 38.05= mode +28.32 24.15-16.64= mode 7.51= mode So, median number and mean number of letters in surnames is 8.05 and 8.32 respectively while modal size of surnames is 7.51.

Q.7. The distribution below gives the weights of 30 students of a class. Find the median weight of the students.

Weight (in kg)	40-45	45-50	50-55	55-60	60-65	65-70	70-75
Number of students	2	3	8	6	6	3	2

Weight (in kgs)	Frequency fi	Cumulative frequency
40-45	2	2
45-50	3	2+3=5
50-55	8	5+8=13
55-60	6	13+6=19
60-65	6	19+6=25
65-70	3	25+3=28
70-75	2	28+2=30
Total (n)	30	***************************************

Here, n=30

So, Cumulative frequency just greater than n2i.e.,302=15 is 19.

It belongs to class interval 55-60

So, Median class =55-60

Lower limit (l) of median class =55

Frequency (f) of median class =6

Cumulative frequency (cf) of median class =13

Class size h=5

Median=l+n2-cff×h

=55+15-136×5

=55+106

=56.666

Hence, median weight is 56.67 kg.

#### Exercise 14.4

Q.1. The following distribution gives the daily income of 50 workers of a factory.

Daily income	100-120	120-140	140-160	160-180	180-200
Number of workers	12	14	8	6	10

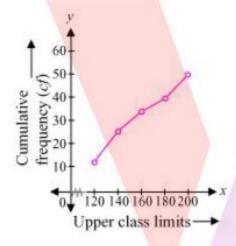
Convert the above distribution to a less than type cumulative frequency distribution, and draw its ogive.

Solution:

We can convert the given distribution table into frequency distribution table of less than type as follows:

Daily income (in ₹) (upper class limits)	Cumulative frequency
Less than 120	12
Less than 140	12+14=26
Less than 160	26+8=34
Less than 180	34+6=40
Less than 200	40+10=50

Now, on x-axis we take upper class limits of class intervals and their respective cumulative frequencies on y-axis. We can draw its ogive as follows:



Q.2. During the medical check-up of 35 students of a class, their weights were recorded as follows:

Weight (in kg)	Number of students	
Less than 38	0	
Less than 40	3	
Less than 42	5	
Less than 44	9	
Less than 46	14	
Less than 48	28	
Less than 50	32	
Less than 52	35	

Draw a less than type ogive for the given data. Hence, obtain the median weight from the graph verify the result by using the formula.

Solution:

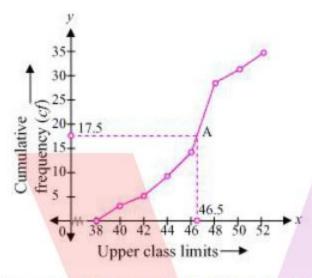
The cumulative frequency distributions of less than type is given as

Weight (in kg)	Number of students
upper class limits	(cumulative frequency)
Less than 38	0
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	Hapter 14 Otationno		
Less than 42	5	W	KRANTADADEM
Less than 44	9	7	KKANTAJADEM
Less than 46	14		
Less than 48	28		
Less than 50	32		
Less than 52	35		

Now, on x-axis we take upper class limits of class intervals and their respective cumulative frequencies on y-axis we can draw its ogive as follows:



Now mark the point A whose ordinate is 17.5 its abscissa is 46.5.

So median of this data is 46.5.

We can see from the table that difference between two consecutive upper-class limits is 2. Now we have to obtain class marks with their respective frequencies as below:

Weight (in kg)	Frequency (f)	Cumulative frequency		
Less than 38	0	0		
38-40	3-0=3	3		
40-42	5-3=2	5		
42-44	9-5=4	9		
44-46	14-9=5	14		
46-48	28-14=14	28		
48-50	32-28=4	32		
50-52	35-32=3	35		
Total (n)	35			

Here, n=35.

So, n2=17.5

Now the cumulative frequency just greater than n2i.e.,352=17.5 is 28. It belongs to class interval 46-48 So, Median class =46-48 Lower class limit (l) of median class =46 Frequency (f) of median class =14 Cumulative frequency (cf) of class preceding median class =14 Class size (h)=2

Median=l+n2-cff×h

=46+17.5-1414×2

=46+3.57 =46+0.5 =46.5 So, median of this data is 46.5. Hence, value of median is verified.

Q.3. The following table gives production yield per hectare of wheat of 100 farms of a village KRANTADADEMY

Production yield (in kg/ha)	50-55	55-60	60-65	65-70	70-75	75-80
Number of farms	2	8	12	24	38	16

Change the distribution to a more than type distribution and draw ogive.

Solution: We can obtain cumulative frequency distribution of more than type as following

Production yield	Cumulative frequency	
more than or equal to 50	100	
more than or equal to 55	100-2=98	
more than or equal to 60	98-8=90	
more than or equal to 65	90-12=78	
more than or equal to 70	78-24=54	
more than or equal to 75	54-38=16	

Now, on x-axis we take upper class limits of class intervals and their respective cumulative frequencies on y-axis we can draw its ogive as following.

